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Structure and frustrated magnetism of the two dimensional triangular lattice antiferromagnet $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$

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A new frustrated triangular lattice antiferromagnet $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ was synthesized by high temperature flux method. The two dimensional triangular lattice is formed by the Ni^{2+} ions with $S = 1$. Its magnetism is highly anisotropic with the Weiss constants $\theta_{CW} = -6.615$ K ($H \perp c$) and -43.979 K ($H \parallel c$). However, no magnetic ordering is present down to 0.3 K, reflecting strong geometric spin frustration. Our heat capacity measurements show substantial residual magnetic entropy existing below 0.3 K at zero field, implying the presence of low energy spin excitations. These results indicate $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ is a potential spin liquid candidate with spin-1.

Keywords: frustrated magnetism, spin liquid, triangle lattice.

PACS: 75.10.Kt, 75.50.Ee, 75.10.Jm

1. INTRODUCTION

The frustrated triangular lattice antiferromagnets (FTLAs) have been widely studied for their relation to quantum spin liquid (QSL) states [1–4]. The well-known $S = 1/2$ QSL material candidates include the FTLAs like $\text{EtMe}_3\text{Sb}[\text{Pd}(\text{dmit})_2]_2$ [5, 6], κ -(BEDT-TTF) $_2\text{Cu}_2(\text{CN})_3$ [7, 8], and YbMgGaO_4 [9]. Spin liquid states may also be realized on $S = 1$ FTLAs such as in $\text{Ba}_3\text{NiSb}_2\text{O}_9$ [10]. Furthermore, the competition of magnetic interactions in FTLA lead to complex phenomena like topological transitions [11], the 1/3-magnetization plateau in Cs_2CuBr_4 [12, 13] and the successive phase transitions in CsNiBr_3 [14]. However, real FTLA materials often suffer with problems from lattice distortion and interlayer interactions, so structurally perfect FTLAs are still highly desirable [15].

Recently, there are reports of FTLA materials in which separated MO_6 ($M =$ transition metal ions) octahedra form a perfect two dimensional triangular lattice [16, 17]. The octahedra do not share any oxygen atom with each other, making the antiferromagnetic interactions moderate. For example, in the spin liquid candidate $\text{Na}_2\text{BaCo}(\text{PO}_4)_2$ the triangular lattice is formed by separated CoO_6 octahedra [16]. Similar layered triangular lattice structures were observed in $\text{A}Ag_2\text{M}[\text{VO}_4]_2$ ($A = \text{Ba, Sr; M} = \text{Co, Ni}$) [18] and $\text{Na}_2\text{BaMV}_2\text{O}_8$ ($M = \text{Ni, Mn, Co}$) [17], but these compounds are ferromagnets except for $\text{Na}_2\text{BaMnV}_2\text{O}_8$ [17]. The distinct magnetic properties of these triangular lattice magnets largely stem from the subtle octahedron crystal field environment and superexchange coupling pathways. It is of great interest to

explore related materials to search for structurally perfect FTLAs.

Here, we report the structure and magnetic properties of a new FTLA material $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$. The crystal has a layered magnetic structure. The Ni^{2+} ions with $S = 1$ form a perfect triangular lattice within the magnetic layers and shows antiferromagnetic magnetism. Its magnetization is highly anisotropic between χ_{\parallel} and χ_{\perp} , demonstrating strong easy-plane type anisotropy. Although its Weiss constants are $\theta_{CW} = -6.615$ K ($H \perp c$) and -43.979 K ($H \parallel c$), no magnetic ordering was observed down to 0.3 K. We also find substantial residual magnetic entropy at zero field. These results reveal the high frustrated magnetism of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$.

2. EXPERIMENT

2.1 SYNTHESIS

Single crystals of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ were synthesized by the flux method. First, 4 mmol BaCO_3 (99.99%, Adamas), 4 mmol NiO (99%, Aldrich), 8 mmol $(\text{NH}_4)_2\text{HPO}_4$ (99%, Adamas), and 60 mmol NaCl (99.5%, Greagent) flux media were fully mixed. The mixture were loaded into a 10 mL alumina crucible, capped with a lid, and heated up at a box-type furnace. After staying at 950 °C for 2 hours, it was cooled to 750 °C at a rate of 3°C/h, and then naturally cooled to room temperature. The obtained crystals were washed in water and separated.

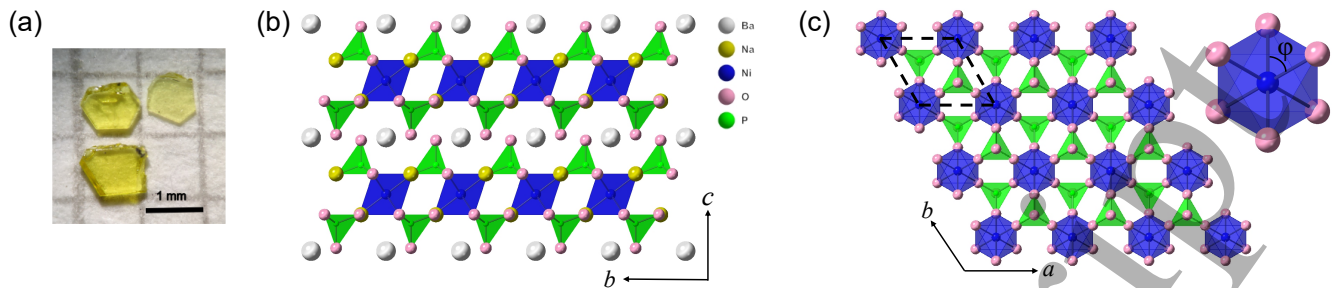


FIG. 1. Crystal structure of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$. (a) Yellow-colored crystals with hexagonal plate-like shape. (b) Layered structure with two dimensional NiO_6 octahedra stacking along the c axis. (c) Triangular magnetic lattice in the ab plane. Right panel: NiO_6 octahedron unit with $\varphi = 93.1(6)^\circ$.

2.2 SINGLE CRYSTAL X-RAY DIFFRACTION

Single crystal X-ray diffraction at 293 K was performed by the Agilent SuperNova diffractometer (Mo K_α radiation, $\lambda = 0.71073$ Å). We used the CrysAlisPro program for X-ray data collection, reduction, and absorption corrections. The SHELXL program package was employed to solve the crystal structure via the direct method[19, 20].

2.3 MAGNETIC SUSCEPTIBILITY AND HEAT CAPACITY MEASUREMENT

The direct-current (dc) magnetic susceptibility measurements were conducted by a MPMS SQUID magnetometer (Quantum Design) with field applied perpendicular or parallel to the c axis. Heat capacity was measured by a Physical Property Measurement System (PPMS, Quantum Design) with a dilution refrigerator insert in magnetic fields up to 9 Tesla.

3. RESULTS AND DISCUSSION

The synthesized hexagonal plate-like single crystals of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ are shown in Fig. 1(a). Single crystal structure determination and refinement indicate the compound crystallizes in a trigonal structure with the space group P-3. The lattice constants are $a = b = 5.2790(3)$ Å, and $c = 6.9596(4)$ Å. Detailed crystal refinement data and atomic coordinates are listed in Tables 1 and 2. It should be noted that our single crystal diffraction did not show detectable site mixing as appeared in some low dimensional magnets. Crystallographic data of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ has been deposited at the Cambridge Crystallographic Data Center (CCDC 2040965).

The resulted crystal structure of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ is illustrated in Figs. 1(b) and 1(c). Ni^{2+} ions ($S = 1$) form two dimensional triangular lattice layers well separated by the nonmagnetic $(\text{PO}_4)^{3-}$, Ba^{2+} , and Na^+ ions. The

TABLE I. Crystal data and structure refinement for $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$.

Empirical formula	$\text{Na}_2\text{BaNi}(\text{PO}_4)_2$
Formula weight	431.94
Temperature	293(2)
Wavelength	0.71073 Å
Crystal system	Trigonal
Space group	P-3
Unit cell dimensions	$a = 5.2790(3)$ Å $b = 5.2790(3)$ Å $c = 6.9596(4)$ Å $\alpha = \beta = 90^\circ$ $\gamma = 120^\circ$
Cell volume	$167.96(2)$ Å ³
Z	1
Calculated density	4.271 g/cm ³
$F(000)$	200.0
2Theta range for data collection	8.914 to 57.938°
Index ranges	$-6 \leq h \leq 3$, $0 \leq k \leq 6$, $0 \leq l \leq 9$
Reflections collected	266
Data/restraints/parameters	266/0/25
Final R indexes [$I \geq 2\sigma(I)$]	$R_1 = 0.0446$ $wR_2 = 0.1152$
Final R indexes [all data],	$R_1 = 0.0465$ $wR_2 = 0.1169$
Goodness-of-fit on F^2	1.102

TABLE II. Atomic coordinates and equivalent isotropic displacement parameters (Å²) for $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$.

Atom	x	y	z	$U(\text{eq})^a$
Ba01	10000	10000	5000	9.7(6)
Ni02	10000	10000	0	8.0(7)
P003	3333.33	6666.67	2563(4)	4.4(8)
Na04	3333.33	6666.67	8201(9)	13.5(12)
O005	3333.33	6666.67	4730(12)	8.6(17)
O006	6422(12)	7733(13)	1793(7)	13.4(15)

^a $U(\text{eq})$ is 1/3 of the trace of the U_{ij} tensor.

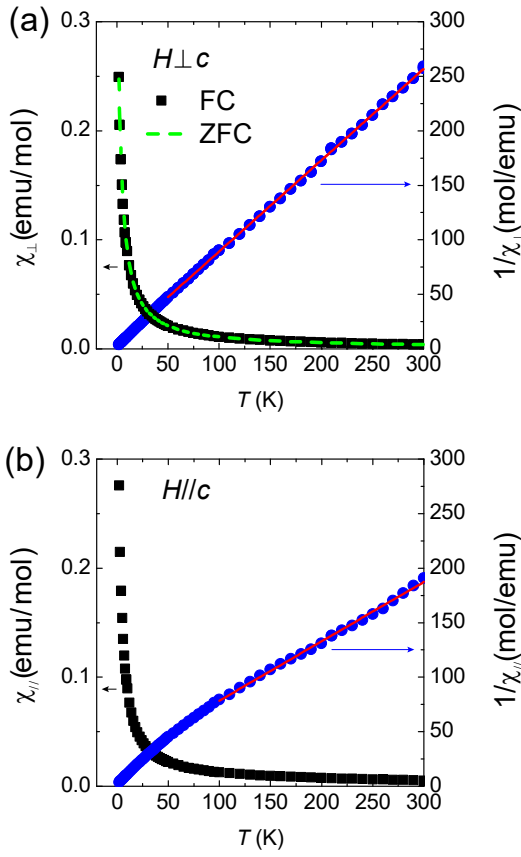


FIG. 2. Magnetic susceptibility of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ with field (a) perpendicular and (b) parallel to c . The FC data (black squares) and ZFC data (green dashed line) are measured under $H = 1000$ Oe and in the temperature range from 2 to 300 K. The red solid lines are the Curie-Weiss law fittings for the $1/\chi(T)$ data (blue dots).

magnetic layers follow a simple A-A-A stacking mode along the c axis (Fig. 1(b)). Each Ni^{2+} ion coordinates with six nearest oxygen atoms to form an octahedron, as shown in the right panel of Fig. 1(c). Within the NiO_6 octahedron, the Ni-O bond lengths are 2.050(17) Å. The octahedron distortion can be characterized by the bond angle φ defined in Fig. 1(c) which is $93.1(6)^\circ$ for $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$, the extent of distortion is similar to that in $\text{Na}_2\text{BaMV}_2\text{O}_8$ ($M = \text{Ni}, \text{Mn}, \text{Co}$) [17]. There is no shared edge or corner between the NiO_6 octahedra and the magnetic interactions between the spins in the triangular lattice propagate along the Ni-[PO_4]-Ni pathway, which should lead to moderate superexchange as observed in related materials [16–18]. In contrast, the interlayer superexchange is along the Ni-[PO_4]-[PO_4]-Ni pathway (Fig. 1(b)) which should be much smaller than the intralayer interaction, making the system a two dimensional magnet.

DC Magnetic susceptibility (χ) of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ single crystal was measured from 2 to 300 K with an external field of $H = 1000$ Oe. The field is applied either perpen-

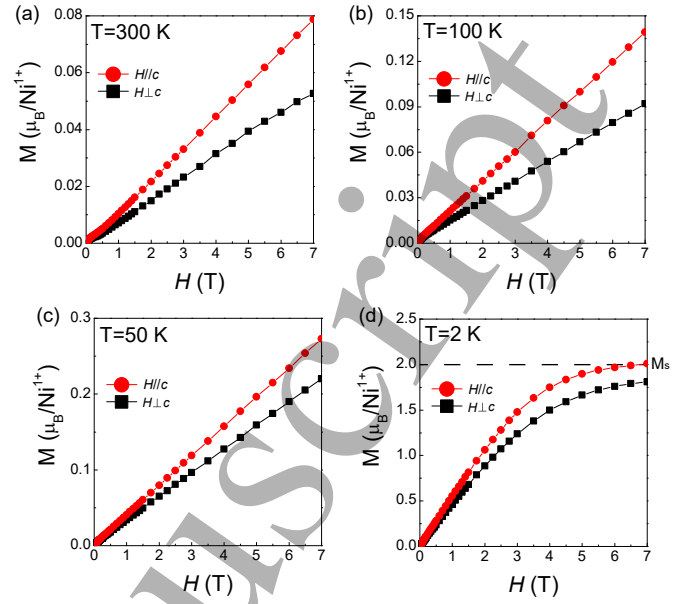


FIG. 3. Magnetization at (a) 300 K, (b) 100 K, (c) 50 K, and (d) 2 K. The dotted line in (d) indicates the saturated magnetization value for a Ni^{2+} ion when only considering the spin moment.

dicular or parallel to the c axis. As can be seen in Fig. 2, χ_\perp and χ_\parallel monotonically increase with lowering temperature, without any signature of phase transitions down to 2 K. The field-cooling (black squares) and zero-field-cooling (ZFC) (green dashed line) data overlap with each other in the measured temperature range (Fig. 2(a)), excluding the spin glass state. The Curie-Weiss law $1/\chi = (T - \theta_{CW})/C$ was used to fit the data between 50 and 300 K for $1/\chi_\perp$, as indicated by the red lines in Fig. 2(a). $1/\chi_\parallel$, however, deviates from the Curie-Weiss law below 100 K, so the data between 100 and 300 K were used for fitting (Fig. 2(b)). The fitting results are $\theta_{CW,\perp} = -6.615$ K, $C_\perp = 1.195$ emu K/mol and $\theta_{CW,\parallel} = -43.979$ K, $C_\parallel = 1.836$ emu K/mol for $\chi_\perp(T)$ and $\chi_\parallel(T)$, respectively. The negative Weiss constants indicate the dominate exchange in $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ is antiferromagnetic. This is in sharp contrast with its analogous compound $\text{Na}_2\text{BaNi}(\text{VO}_4)_2$ which is a ferromagnet with transition temperature at 8.4 K [17].

The significant difference between $\theta_{CW,\perp}$ and $\theta_{CW,\parallel}$ reveals strong magnetic anisotropy in $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ which reflects strong anisotropic exchange interactions in its spin Hamiltonian. Similar anisotropic magnetism has been found in related layered magnets like $\text{Na}_2\text{BaMV}_2\text{O}_8$ ($M = \text{Ni}, \text{Mn}, \text{Co}$) [17], $\text{BaCo}_2(\text{AsO}_4)_2$ [21] and $\alpha\text{-RuCl}_3$ [22]. To further reveal the magnetic anisotropy, we measured magnetization at $T = 300, 100, 50,$ and 2 K with field perpendicular or parallel to the c axis, the results are shown in Fig. 3. In Figs. 3(a-d), both M_\parallel and M_\perp increase linearly from 0 to 7 T with M_\parallel apparently larger than M_\perp . The anisotropy can still be observed at 300 K

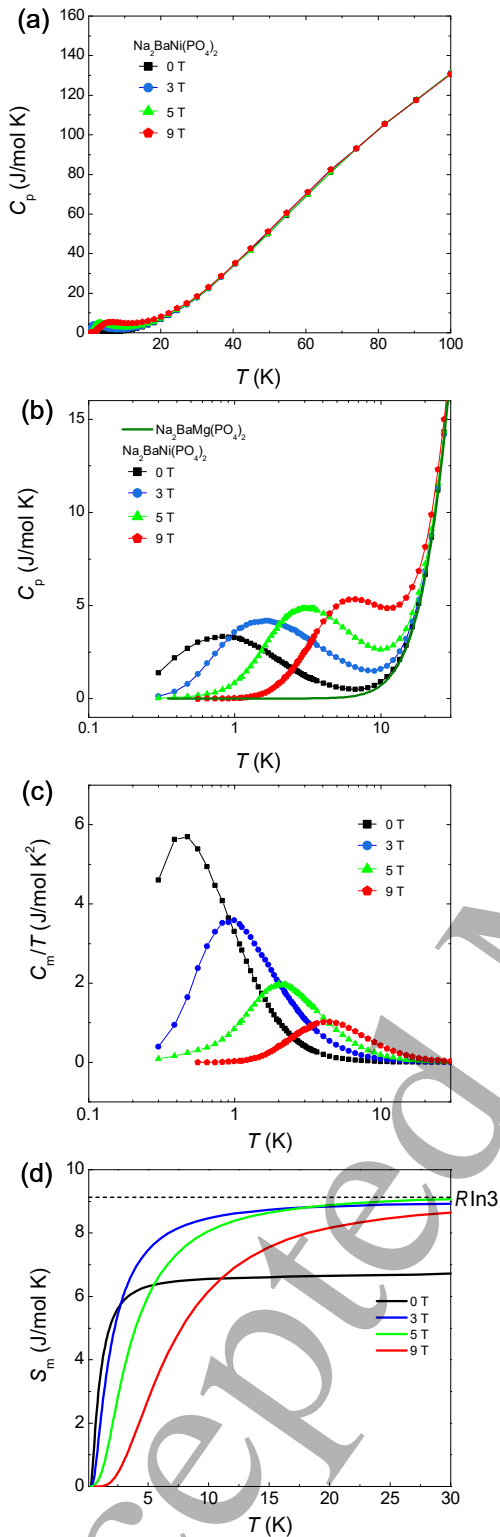


FIG. 4. (a) Heat capacity of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ below 100 K. (b) Heat capacity in the temperature range from 0.3 to 30 K. The magnetic fields are at 0, 3, 5, and 9 T. The heat capacity of $\text{Na}_2\text{BaMg}(\text{PO}_4)_2$ (olive solid line) was obtained from ref. 16. (c) Temperature dependences of C_m/T at different fields. (d) Integrated magnetic entropy S_m in $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$. $R\ln 3$ is the total magnetic entropy for a $S = 1$ magnet.

(Fig. 3(a)), indicating the size of anisotropic excitation gap should be comparable to the thermal energy.

At 2 K, M is proportional to H at lower fields and tends to saturate at high fields (Fig. 3(d)). The theoretical saturated magnetization M_s is $gS\mu_B$. M_s equals to $2\mu_B/\text{Ni}^{2+}$ if only considering the spin moment, consistent with the observed value. The magnetization curve at all measured temperatures have no anomaly, indicating absence of magnetic transitions or long range orderings. The 1/3 magnetization plateau stemming from quantum spins in triangular lattice is also absent here, implying $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ may be treated as a classic FTLA.

The heat capacity data of $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ at magnetic fields up to 9 T are presented in Fig. 4. The heat capacity above 30 K are field independent and do not show any anomaly related to phase transitions (Fig. 4(a)). However, the low temperature data exhibit a broad peak that shift to higher temperatures with stronger fields (Fig. 4(b)). This feature is typical in several $S = 1$ QSL candidates such as $[\text{NH}_4]_2[\text{C}_7\text{H}_{14}\text{N}][\text{V}_7\text{O}_6\text{F}_{18}]$ [23] and $\text{Ba}_3\text{NiSb}_2\text{O}_9$ [10]. Some $S = 1/2$ QSL candidates such as YbMgGaO_4 and $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ also exhibit similar broad feature in heat capacity at low temperature [9, 16].

Magnetic heat capacity C_m is sensitive to the low energy spin excitations. We used the heat capacity of $\text{Na}_2\text{BaMg}(\text{PO}_4)_2$ as the phonon contribution in $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ since they are isostructural (solid line in Fig. 4(b), the data was got from ref. 16). The temperature dependences of C_m/T at different fields are displayed in Fig. 4(c). The magnetic entropy $S_m(T)$ was subsequently got by integrating C_m/T from ~ 0.3 K to T (Fig. 4(d)). For a $S = 1$ magnet, the total magnetic entropy is $R\ln 3$, where R is the ideal gas constant. As can be seen in Fig. 4(d), S_m is nearly saturated by 30 K. The zero field magnetic entropy is only $0.74R\ln 3$ at 30 K, indicating substantial residual magnetic entropy below 0.3 K. The zero point entropy usually comes from strong spin fluctuations in disordered systems which lift the degeneracy of ground state. By applying magnetic field, the energy barriers of spin reorientations will be enhanced, making S_m increase to its conventional value $R\ln 3$, consistent with our experimental observed value at magnetic fields (Fig. 4(d)).

It is interesting to compare $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ with its analog compound $\text{Na}_2\text{BaCo}(\text{PO}_4)_2$, the Co-based triangular lattice antiferromagnet [16]. Both compounds have the $\text{MO}_6\text{-PO}_4\text{-PO}_4\text{-MO}_6$ ($M = \text{Ni}, \text{Co}$) stacking structure along the c axis. Their lattice constants only have slight differences. For instance, the closest Ni-Ni distance is 5.279\AA in $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ and the closest Co-Co distance is 5.319\AA in $\text{Na}_2\text{BaCo}(\text{PO}_4)_2$. The similarities in structure result in moderate antiferromagnetic couplings in both compounds. However, the magnetic anisotropy in $\text{Na}_2\text{BaCo}(\text{PO}_4)_2$ is insignificant with $\Theta_{CW,\perp} = -31.9$ K and $\Theta_{CW,\parallel} = -32.6$ K, in sharp contrast with the strong magnetic anisotropy in $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$. The anisotropy

is closely related to the angular distributions of the outmost $3d$ electron orbits and largely depends on the $3d$ electron configurations as well as the octahedra crystal field. Further study by inelastic neutron scattering on $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ is necessary to determine its detailed exchange couplings and anisotropic spin hamiltonian.

4. CONCLUSION

In summary, we have synthesized a new antiferromagnet $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$. From single crystal X-ray diffraction we find its crystal structure has a perfect two dimensional triangular lattice formed by Ni^{2+} ions. The Weiss constants are -6.615 K and -43.979 K for field perpendicular and parallel to the c axis, respectively. However, magnetic ordering is absent down to 0.3 K and up to 9 T. So we conclude $\text{Na}_2\text{BaNi}(\text{PO}_4)_2$ is a new FLTA that could be used for study of novel states such as QSL in frustrated magnets.

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